

Course Syllabus**I. General Information**

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| Course name | Foundations of probabilistic methods |
| Programme | Informatics |
| Level of studies (BA, BSc, MA, MSc, long-cycle MA) | BSc |
| Form of studies (full-time, part-time) | full-time |
| Discipline | Informatics |
| Language of instruction | Polish |

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| Course coordinator/person responsible | Dr Kamil Powroźnik |
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| Type of class (<i>use only the types mentioned below</i>) | Number of teaching hours | Semester | ECTS Points |
|---|--------------------------|----------|-------------|
| lecture | 30 | III | 5 |
| tutorial | | | |
| classes | 30 | III | |
| laboratory classes | | | |
| workshops | | | |
| seminar | | | |
| introductory seminar | | | |
| foreign language classes | | | |
| practical placement | | | |
| field work | | | |
| diploma laboratory | | | |
| translation classes | | | |
| study visit | | | |

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| Course pre-requisites | Mathematical analysis (numerical sequences and series, differential and integral calculus of functions of one and several variables) |
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II. Course Objectives

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| C1 - Studying mathematical methods used for the description of random phenomena |
| C2 - Learning methods for calculating probabilities of random events, determining distributions of random variables and finding numerical parameters of probability distributions |
| C3 - Learning about different modes of convergence of random variables |
| C4 - Calculating the characteristic functions (Fourier transforms) |
| C5 - Learning the basic limit theorems of probability theory |

III. Course learning outcomes with reference to programme learning outcomes

| Symbol | Description of course learning outcome | Reference to programme learning outcome |
|----------------------------|--|---|
| KNOWLEDGE | | |
| W_01 | Students give various definitions of probability and build mathematical models describing random phenomena and random experiments | K_W09 |
| W_02 | Students list the most important discrete and continuous probability distributions | K_W09 |
| W_03 | Students quote the basic theorems of probability theory | K_W09 |
| SKILLS | | |
| U_01 | Students use in practice various probability definitions, the law of total probability and the Bayes formula, examine the independence of random variables, calculate parameters of distributions for discrete and continuous random variables, calculate covariances and correlation coefficients, find equations of regression lines | K_U22 |
| U_02 | Students recognize probability distributions based on characteristic functions | K_U22 |
| U_03 | Students apply probabilistic methods for solving problems from various fields | K_U22 |
| SOCIAL COMPETENCIES | | |
| K_01 | Students formulate opinions on selected practical issues using tools of probability theory | K_K01 |

IV. Course Content

1. Elements of combinatorics.
2. Random experiment, sample space, elementary events, random events.
3. Classical and geometrical definitions of probability. Examples of applications.
4. Axioms of probability. Properties of probability. Construction of a probability measure.
5. Independence of a random events. Conditional and total probability. Bayes formula. Bernoulli scheme.
6. Random variable and its distribution. Discrete and continuous variables. Probability and density functions. Cumulative distribution function of a random variable.
7. Basic distributions of discrete and continuous type. Standard normal distribution and its applications.
8. Main characteristics of random variables and their properties (expectation, variance, moments and central moments).
9. Characteristic function and its properties. The inversion formula. Levy-Cramer's theorem. A relation between a characteristic function and moments.
10. Multivariate random variables. Marginal and conditional distributions. Independence of a random variables.
11. Covariance and correlation coefficient, properties of a correlation coefficient. Lines of regression..
12. Various kinds of convergence of random variables. Relationships between various modes of convergence.

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| 13. Limit theorems (such as Laws of large numbers, Poisson limit theorem, Central Limit Theorem). |
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V. Didactic methods used and forms of assessment of learning outcomes

| Symbol | Didactic methods <i>(choose from the list)</i> | Forms of assessment <i>(choose from the list)</i> | Documentation type <i>(choose from the list)</i> |
|----------------------------|---|--|---|
| KNOWLEDGE | | | |
| W_01 | Conventional lecture, guided practice elements of e-learning | Written exam, written test | Evaluated exam, evaluated test |
| W_02 | Conventional lecture, guided practice, elements of e-learning | Written exam, written test | Evaluated exam, evaluated test |
| W_03 | Conventional lecture, guided practice, elements of e-learning | Written exam, written test | Evaluated exam, evaluated test |
| SKILLS | | | |
| U_01 | Practical classes, guided practice, elements of e-learning | Written exam, written test | Evaluated exam, evaluated test |
| U_02 | Practical classes, guided practice, elements of e-learning | Written exam, written test | Evaluated exam, evaluated test |
| U_03 | Practical classes, guided practice, elements of e-learning | Written exam, written test | Evaluated exam, evaluated test |
| SOCIAL COMPETENCIES | | | |
| K_01 | Discussion, practical classes | Written exam, written test | Evaluated exam, evaluated test |

VI. Grading criteria, weighting factors.....

Lecture:

Written exam divided on two parts:

- practical - verifying the ability to apply in practice the knowledge gained during lectures and classes,
- theoretical - checking the theoretical knowledge acquired during the lecture.

Evaluation criteria :

[0-50%) points - unsatisfactory (2)

[50% -60%] - satisfactory (3)

[60% -70%) - satisfactory plus (3.5)

[70% -80%) - good (4)

[80% -90%) - good plus (4.5)

[90% -100%] - very good (5)

Classes:

Two written tests. To get a credit student should obtain from both tests minimum 50% of points.

Evaluation criteria :

[0-50%) points - unsatisfactory (2)

[50% -60%] - satisfactory (3)

[60% -70%) - satisfactory plus (3.5)

[70% -80%) - good (4)

[80% -90%) - good plus (4.5)

[90% -100%] - very good (5)

The detailed description of assessment is given during the first lecture/classes.

VII. Student workload

| Form of activity | Number of hours |
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| Number of contact hours (with the teacher) | 90 |
| Number of hours of individual student work | 60 |

VIII. Literature

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| Basic literature |
| <ol style="list-style-type: none"> 1. A. Borowkow, "Rachunek prawdopodobieństwa", PWN 1977. 2. J. Jakubowski, R. Sztencel, "Wstęp do teorii prawdopodobieństwa", Script 2002. 3. P. Billingsley, "Prawdopodobieństwo i miara", PWN 1967. 4. W. Feller, "Wstęp do rachunku prawdopodobieństwa", t. I-II, PWN 1969. 5. M. Fisz, "Rachunek prawdopodobieństwa i statystyka matematyczna", PWN 1967. 6. Notatki z wykładu. |
| Additional literature |
| <ol style="list-style-type: none"> 1. W. Krysicki i in., "Rachunek prawdopodobieństwa i statystyka matematyczna w zadaniach", t. I-II, PWN 1997. 2. T. Gerstenkorn, T. Śródka, "Kombinatoryka i rachunek prawdopodobieństwa", PWN 1978. |